# Calculation of Secondary Electron Emission Yield $\gamma$ From MgO Surface

Yasushi Motoyama and Fumio Sato

Abstract—Secondary electron emission yield  $\gamma$  values for rare-gas particles (He, Ne, Ar, Kr, and Xe ions of atoms and molecules, metastable atoms, and excimers) of MgO deposited under optimum conditions for the highest  $\gamma$  values were calculated assuming the Auger transitions between the valence band, and the F (oxygen ion vacancy + two electrons) and  $F^+$  (oxygen ion vacancy + one electron) centers in the MgO surface. These calculated  $\gamma$  values are probably the same as  $\bar{\gamma}$  values for MgO used in practice. As for combination of the MgO with these rare-gas particles, all the calculated  $\gamma$  values fall to nonzero; resonance neutralization cannot occur for the rare-gas particles except Ne and Xe<sub>2</sub> ions. Therefore,  $\gamma$  values of the MgO for these rare-gas particles, other than Ne and Xe2 ions, are determined only by Auger neutralization. For Ne and Xe2 ions, the influence of resonance neutralization effect on calculated  $\gamma$  values of ions is small. Therefore,  $\gamma$  values of the MgO for Ne and Xe<sub>2</sub> ions are also almost determined only by Auger neutralization. The  $\gamma$ values for the ions of atoms are a little larger than those for the ions of molecules. The  $\gamma$  values of the metastable atoms are also a little larger than those of the excimers. As for MgO without defect states, calculated  $\gamma$  values of Ar, Kr, and Xe ions of atoms and molecules fall to zero; calculated  $\gamma$  value of  $Xe_2$  excimer at the lowest continuous spectrum also falls to zero; these calculated  $\gamma$  values for MgO without defect states are probably the lowest values theoretically. As for rare-gas ions of atoms, the calculated  $\gamma$  values have been compared with experimental results reported previously. These results will be useful in detailed investigations into the mechanism of discharge of plasma display panels (PDPs).

Index Terms—Plasma display panels (PDPs), protective layer, MgO, secondary electron emission yield  $\gamma,F$  center.

### I. INTRODUCTION

THE secondary electron emission yield  $\gamma$  of the cathode is an important factor for improving the discharge characteristics of plasma display panels (PDPs) because of its close relationship with the discharge voltage. In PDPs, the electrodes are covered with glass, which is usually coated with an MgO film because of its low breakdown voltage and good durability [1].

The theoretical  $\gamma$  values of MgO without energy bands in the bandgap for Ne and Ar ions were calculated [2] from Hagstrum's theory [3], [4]. For an insulator without energy bands in the band gap, we have calculated the generalized relations between the  $\gamma$  values and physical parameters from Hagstrum's theory [2]–[4] and showed that the  $\gamma$  values of MgO without energy bands in the bandgap for Kr and Xe ions fall to zero [5], [6]. Additionally, the  $\gamma$  values of MgO with one defect state in the bandgap were calculated theoretically

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The authors are with Science and Technical Research Laboratories, NHK (Japan Broadcasting Corporation), 157-8510 Tokyo, Japan.
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[7], although the energy level of the defect state used in this calculation was determined arbitrarily. In order to investigate the energy bands in the band gap, the cathodoluminescence (CL) spectra of MgO were measured. The CL spectra from these energy bands depended on the substrate temperature during MgO film deposition [8]. Moreover, the influence of the oxygen feed during MgO film deposition on the CL spectra has been reported [9]. We also measured CL spectra of MgO films, deposited at several oxygen partial pressures and observed CL peaks at around 520 and 370 nm [10]. It has been suggested that the 525- and 375-nm bands are probably due to the F and  $F^+$ centers, respectively, in the MgO surface [11], [12]. The breakdown voltages decreased with increasing CL intensities from the F and  $F^+$  centers, especially from the  $F^+$  centers. These result suggested that the  $\gamma$  values also increase with increasing numerical densities of the F and  $F^+$  centers, especially for  $F^+$ centers [10]. The  $\gamma$  values of MgO for Ne and Xe ions, which include the F and  $F^+$  bands, were calculated assuming that the probabilities of transitions are proportional to the measured CL intensities from the F and  $F^+$  bands in the MgO. Here, the  $\gamma$ values of the MgO film deposited at the oxygen partial pressure  $(1.2 \times 10^{-4} \text{ torr})$  and substrate temperature (300 °C) reach the highest [10]. Throughout this paper, we call these deposition conditions the optimum conditions.

In this paper, for rare-gas ions and metastable atoms, the  $\gamma$  values of MgO deposited under the optimum conditions were calculated. Moreover, for ionized and metastable rare-gas molecules, the  $\gamma$  values of MgO deposited under the optimum conditions were also calculated. These calculated  $\gamma$  values, except  $\gamma$  values of Ne and Xe ions, have not been reported. These calculated  $\gamma$  values of MgO deposited under the optimum conditions were compared with those of MgO without energy bands in the band gap. Regarding rare-gas ions, experimental  $\gamma$  values were previously reported. Therefore, the calculated  $\gamma$  values of MgO were compared with these experimental results.

### II. DERIVATION OF SECONDARY ELECTRON EMISSION YIELD $\gamma$

### A. Conditions for Secondary Electron Emission

According to the research by Hagstrum [3], [4], it is known that secondary electron emission by low-velocity ions, as in conventional gas-discharge phenomena [13], does not depend on kinetic energy but mostly on the potential (internal) energy of the ion. In this case, the mechanism of electron emission consists of the following two processes:

- 1) Auger neutralization (one step);
- resonance neutralization + Auger deexcitation (two steps).

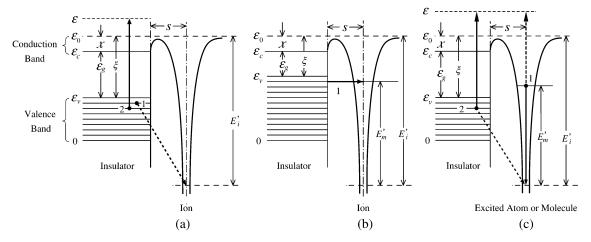


Fig. 1. Schematic diagram illustrating electronic transitions at an insulator surface. (a) Auger neutralization of an ion. (b) Resonance neutralization of an ion. (c) Auger deexcitation of an excited atom or molecule.

Here, Auger neutralization, resonance neutralization (the inverse of resonance ionization), and Auger deexcitation are tunnel effects, as shown in Fig. 1(a)–(c), where the latter two are concerned with the excited state of the atom, especially the metastable states. The notions of physical parameters used in Fig. 1, as defined in Table I, are also used throughout the paper. When defect states do not exist in the band gap of an insulator, the necessary condition that 1) and 2) occur is given by  $E_i' \geq \xi + \varepsilon_g$  and  $\varepsilon_0 \geq E_i' - E_m' \geq \xi$ . Therefore, depending on the combination of an insulator and a gas, the following cases exist: only 1) or 2) occurs; both 1) and 2) occur; or neither 1) nor 2) occur. Moreover, the necessary conditions that the electron can be ejected by the above mechanisms are (i)  $E_i' \geq 2\xi$  and (ii)  $E_m' \geq \xi$ .

## B. Secondary Electron Emission Yield $\gamma^N$ Based on Auger Neutralization

The electron energy distribution function  $n(\varepsilon)$  in the valance band of the insulator is given by the product of the state density,  $\rho(\varepsilon)$ , and the Fermi–Dirac distribution function,  $f(\varepsilon)$ , where the latter can be regarded as a step function at room temperature, that is,  $f(\varepsilon)=1$  for  $\varepsilon\leq\varepsilon_F$  and  $f(\varepsilon)=0$  for  $\varepsilon\geq\varepsilon_F$ . As in Fig. 1(a), when electron 1 moves to the ground state of an atom and electron 2 is excited at the same time, the energy distribution  $E_i'(\varepsilon)$  of the excited electron is given by the following expression by using the Auger transform  $T[\cdot]$  defined in it, with the assumption that the matrix element of this transition is independent of the energies of these electrons [4]

$$N_{i}'(\varepsilon) \propto \rho_{0}(\varepsilon) \int_{0}^{\varepsilon_{v}} \int_{0}^{\varepsilon_{v}} n(\varepsilon_{1}) n(\varepsilon_{2})$$

$$\times \delta(\varepsilon - \varepsilon_{1} - \varepsilon_{2} + \varepsilon_{0} - E_{i}') d\varepsilon_{1} d\varepsilon_{2}$$

$$\equiv \rho_{0}(\varepsilon) T \left[ \frac{\varepsilon + \varepsilon_{0} - E_{i}'}{2} \right]$$
(1)

where,  $\delta(\cdot)$  is the Dirac delta function and indicates the conservation of energy, and  $\rho_0(\varepsilon)$  is the state density for the excited electron and is considered to be proportional to  $(\varepsilon - \varepsilon_c)^{1/2}$ . Next, for an electron, thus excited, to escape from the solid, it is necessary that  $\varepsilon > \varepsilon_0$ . Assuming that this escape probability

TABLE I
DEFINITION OF PHYSICAL PARAMETERS

arepsilon : energy of an excited electron

 $oldsymbol{arepsilon}_0$  : energy of vacuum level

 $\mathcal{E}_c$ : energy of bottom of conduction band

 $\mathcal{E}_{v}$ : energy of top of valence band

 $\mathcal{E}_f$ : energy of top of F band from the vacuum level

 $\mathcal{E}_{f+}$ : energy of top of  $F^+$  band from the vacuum level

 $\varepsilon_g \equiv \varepsilon_c - \varepsilon_v$  : band gap

 $\chi \equiv \varepsilon_0 - \varepsilon_c$  : electron affinity

 $\xi \equiv \chi + \varepsilon_g \equiv \varepsilon_0 - \varepsilon_v$ 

 $E_i'$ : ionization energy at a distance s from the solid

 $E_{\scriptscriptstyle m}^{\prime}$  : excitation energy at a distance s from the solid surface

is  $P_e(\varepsilon)$ , we obtain the following expression for the secondary electron emission yield,  $\gamma^{/N}$ , at a distance s

$$\gamma'^{N} = \int_{\max\{E'_{i} - \varepsilon_{0}, \varepsilon_{0}\}}^{E'_{i} - 2\xi + \varepsilon_{0}} P_{e}(\varepsilon) \sqrt{\varepsilon - \varepsilon_{c}} T \left[ \frac{\varepsilon + \varepsilon_{0} - E'_{i}}{2} \right] d\varepsilon$$

$$/ \int_{\max\{E'_{i} - \varepsilon_{0}, \varepsilon_{c}\}}^{E'_{i} - 2\xi + \varepsilon_{0}} \sqrt{\varepsilon - \varepsilon_{c}} T \left[ \frac{\varepsilon + \varepsilon_{0} - E'_{i}}{2} \right] d\varepsilon \quad (2)$$

where  $P_e(\varepsilon)$  for the electron excited by Auger neutralization is not isotropic. By taking this into consideration, the following formula has been proposed, introducing parameters  $\alpha$  and  $\beta$  [4]

$$P_e(\varepsilon) = \frac{1}{2} [1 - (\varepsilon_0/\varepsilon)^{\beta}]^{\alpha}, \quad \varepsilon > \varepsilon_0.$$
 (3)

Hagstrum determined  $\alpha=0.248, \beta=1.0$  by adjusting to correspond with the experimental results of He<sup>+</sup> for Ge. These values are also used in the present calculation. Since a transition occurs when an ion travels a long way to the solid surface, the desired  $\gamma^N$  must be an average of  $\gamma'^N$  over s. In practice, however, it is known from experiments that transitions occur collectively at a certain distance  $s=s_m$  [3], [4]. Therefore,

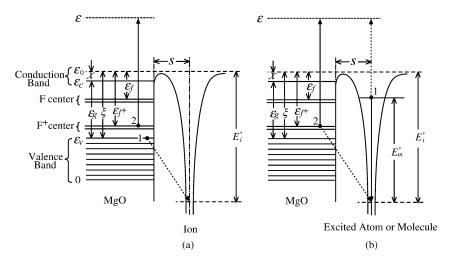


Fig. 2. Schematic diagram illustrating electronic transitions at an MgO surface that includes F and  $F^+$  bands. (a) Auger neutralization of an ion. (b) Auger deexcitation of an excited atom or molecule.

substituting the ionization energy at  $s = s_m$  for  $E_i$ ', we can obtain a good approximation of  $\gamma^N$ .

In practical calculations, the state density  $\rho(\varepsilon)$  in  $n(\varepsilon)$  must be given. But this varies, depending on the kind of insulator. This being the case, the calculations here are performed for two cases, a flatband and a parabolic band, to study the influence of the state-density profile on the  $\gamma$  value. Furthermore, by putting  $x \equiv \varepsilon/\varepsilon_0$  and  $\sigma \equiv \varepsilon_c/\varepsilon_0$  to normalize the variables, we obtain the following formula from (2)

$$\gamma^{\prime N} = \int_{\max\{\alpha_i, 1\}}^{\beta_i} P_e^*(x) \sqrt{x - \sigma} T^*(x) dx$$

$$/ \int_{\max\{\alpha_i, \sigma\}}^{\beta_i} \sqrt{x - \sigma} T^*(x) dx. \quad (4)$$

Where  $\alpha_i \equiv E_i'/\varepsilon_0 - 1$ ,  $\beta_i \equiv (E_i' - 2\xi)/\varepsilon_0 + 1$  and  $P_e^*(\varepsilon) \equiv \frac{1}{2}(1 - x^{-\beta})^{\alpha}$ . The function  $T^*[x]$ , which is finite only when  $\alpha_i < x < \beta_i$ , is given as follows, depending on the state density assumed for flatband

$$T^*[x] = x - \alpha_i, \quad \alpha_i < x \le (\alpha_i + \beta_i)/2$$
  

$$T^*[x] = \beta_i - x, \quad (\alpha_i + \beta_i)/2 < x < \beta_i.$$
 (5)

### C. Secondary Electron Emission Yield $\gamma^D$ Based on Auger Deexcitation

When an ion approaches a solid surface and resonance neutralization occurs, the ion becomes an excited atom. After this process, unless resonance ionization occurs with the condition  $E'_i - E'_m < \chi$  for a smaller distance s, the excited atom is considered to return to the ground state by Auger deexcitation. Accordingly, as a component of the secondary electron emission yield,  $\gamma_i$ , by an ion, we have to consider  $\gamma^D$  as well as the above-mentioned  $\gamma^N$ . Specifically, when the transition ratio of Auger neutralization to resonance neutralization is g to (1-g), then  $\gamma_i$  is given by

$$\gamma_i = g\gamma^N + (1 - g)\gamma^D. \tag{6}$$

TABLE II
BAND PARAMETERS OF MgO USED IN THIS STUDY

| Energy (eV) | $\mathcal{E}_{_{\scriptscriptstyle \mathcal{V}}}$ | $\epsilon_{\scriptscriptstyle g}$ | χ    | $\mathcal{E}_0$ | $oldsymbol{arepsilon}_f$ | $\varepsilon_{\scriptscriptstyle f+}$ |
|-------------|---|-----------------------------------|------|-----------------|--------------------------|---------------------------------------|
| MgO         | 5.0   | 6.8                               | 0.85 | 12.65           | 3.8                      | 5.3                                   |

On the other hand, in the secondary electron emission yield  $\gamma_m$  by a metastable atom, this  $\gamma^D$  is considered to be the main component, namely,  $\gamma_m = \gamma^D$ .

Similarly to the procedure for obtaining  $\gamma^N$ , the energy distribution,  $N'_i(\varepsilon)$ , of the excited electron is given by

$$N_i'(\varepsilon) \propto \rho_0 \int_0^{\varepsilon_v} n(\varepsilon_2) \delta(\varepsilon_2 + E_m' - \varepsilon) d\varepsilon_2$$
  
=  $\rho_0(\varepsilon) n(\varepsilon - E_m')$ . (7)

Also, in Auger deexcitation, by adopting the same escape probability as in Auger neutralization and the excitation energy  $E'_m$  at  $s=s_m, \gamma'^D$  is obtained as follows:

$$\gamma'^{D} = \int_{\max\{E'_{m}, \varepsilon_{0}\}}^{E'_{m} - \xi + \varepsilon_{0}} P_{e}(\varepsilon) \sqrt{\varepsilon - \varepsilon_{c}} n(\varepsilon - E'_{m}) d\varepsilon$$

$$/ \int_{\max\{E'_{m}, \varepsilon_{c}\}}^{E'_{m} - \xi + \varepsilon_{0}} \sqrt{\varepsilon - \varepsilon_{c}} n(\varepsilon - E'_{m}) d\varepsilon. \quad (8)$$

Here, as in Auger neutralization, assuming  $\rho(\varepsilon)$  is a flatband, and putting  $x \equiv \varepsilon/\varepsilon_0$  and  $\sigma \equiv \varepsilon_c/\varepsilon_0$ , we obtain

$$\gamma^{\prime D} = \int_{\max\{\alpha_m, 1\}}^{\beta_m} P_e^*(x) \sqrt{x - \sigma} n^*(x) dx$$

$$/ \int_{\max\{\alpha_m, \sigma\}}^{\beta_m} \sqrt{x - \sigma} n^*(x) dx \quad (9)$$

where  $\alpha_m \equiv E_m'/\varepsilon_0$ , and  $\beta_m \equiv (E_m'-\xi)/\varepsilon_0+1$ . The function  $n^*(x)$ , which is finite only when  $\alpha_m < x < \beta_m$ , is given as follows, depending on the state density assumed for flatband

$$n^*(x) = 1, \quad \alpha_m < x < \beta_m. \tag{10}$$

| $E_i'(eV)$                         | $\gamma_{\!f\!f}$ | $\gamma_{f+f}$ | $\gamma_{\!ff}$ | $\gamma_{f+f+}$ | $\gamma_{\!f \nu}$ | $\gamma_{_{\!v\!f}}$ | $\gamma_{f+\nu}$ | $\gamma_{\nu f^+}$ | $\gamma_{\nu\nu}$ |
|------------------------------------|-------------------|----------------|-----------------|-----------------|--------------------|----------------------|------------------|--------------------|-------------------|
| He <sup>+</sup> 23.27              | 0.472             | 0.469          | 0.460           | 0.456           | 0.420              | 0.459                | 0.413            | 0.441              | 0.329             |
| ${\rm He_2}^+$ 22.23               | 0.470             | 0.467          | 0.457           | 0.453           | 0.415              | 0.455                | 0.407            | 0.435              | 0.307             |
| Ne <sup>+</sup> 20.36              | 0.466             | 0.462          | 0.451           | 0.446           | 0.405              | 0.446                | 0.395            | 0.421              | 0.257             |
| $Ne_{2}^{+}$ 20.33                 | 0.466             | 0.462          | 0.451           | 0.445           | 0.405              | 0.446                | 0.394            | 0.420              | 0.256             |
| Ar <sup>+</sup> 14.80              | 0.445             | 0.435          | 0.419           | 0.401           | 0.346              | 0.357                | 0.226            | 0.234              | 0                 |
| Ar <sub>2</sub> <sup>+</sup> 14.50 | 0.444             | 0.432          | 0.416           | 0.396           | 0.334              | 0.344                | 0.206            | 0.215              | 0                 |
| Kr <sup>+</sup> 14.00              | 0.440             | 0.427          | 0.410           | 0.387           | 0.299              | 0.311                | 0.165            | 0.174              | 0                 |
| $Kr_2^+$ 12.87                     | 0.431             | 0.412          | 0.394           | 0.358           | 0.197              | 0.220                | 0                | 0                  | 0                 |
| Xe <sup>+</sup> 11.33              | 0.411             | 0.377          | 0.357           | 0.258           | 0                  | 0                    | 0                | 0                  | 0                 |
| $Xe_{2}^{+}$ 11.02                 | 0.406             | 0.366          | 0.345           | 0.165           | 0                  | 0                    | 0                | 0                  | 0                 |

TABLE III CALCULATED  $\gamma$  VALUES BASED ON AUGER NEUTRALIZATION BETWEEN THE VALENCE BAND AND THE F AND  $F^+$  BANDS OF MgO FOR RARE-GAS IONS

### III. DERIVATION OF SECONDARY ELECTRON EMISSION YIELD $\gamma$ OF MgO WITH DEFECT STATES

In order to include the effects of the F and  $F^+$  bands in  $\gamma^N$ , we have to consider Auger transitions between the valence band, and the F and  $F^+$  bands. Fig. 2(a) shows a schematic diagram of Auger neutralization of an ion at the MgO surface that possesses the F and  $F^+$  bands. The notions of physical parameters used in Fig. 2 are also defined in Table I. The secondary electron emission yields  $\gamma^N$  derived from these transitions were calculated using (4). The band parameters of MgO used in these calculations are shown in Table II, where  $\varepsilon_v = 5.0$  eV,  $\varepsilon_q = 6.8$  eV, and  $\chi = 0.85$  eV [2]. In general, it is not easy to determine the values of  $\varepsilon_f$  and  $\varepsilon_{f^+}$  using CL, due to the Stokes shifts. Therefore, the values of  $\varepsilon_f = 3.8$  eV and  $\varepsilon_{f^+} = 5.3$  eV, as shown in Table II, were assumed, based on the results of the calculations which were made using the embedded cluster method [14]. Table III shows the calculated  $\gamma^N$  values, based on Auger neutralization between the valence band, and the F and  $F^+$  bands of MgO for He, Ne, Ar, Kr, and Xe ions of atoms and molecules. Here, as in Fig. 2(a), when an electron 1 in the valence band moves to the ground state and an electron 2 in the  $F^+$  band is excited at the same time, the symbol for this secondary electron emission yield is assigned as  $\gamma_{vf^+}$ , for example. The symbols for the other secondary electron emission yields are also represented by similar procedures. In practical calculations, the estimated values of  $E'_i$  for He, Ne, Ar, and Xe ions are 23.27, 20.36, 14.80, and 11.33 eV, respectively, [7], [15]. As for Kr,  $He_2$ ,  $Ne_2$ ,  $Ar_2$ ,  $Kr_2$ , and  $Xe_2$  ions, the values of  $E'_i$  are 14.00, 22.23, 20.33, 14.50, 12.87, and 11.02 eV, respectively [16], [17] on the assumption that the values of  $E'_i$  are equal to those of  $E_i$  (free space ionization energy). The widths of the F and  $F^+$ bands are assumed to be 0.3 eV. For Xe and Xe2 ions, the values of  $\gamma_{\rm fv}, \gamma_{\rm vf}, \gamma_{f^+v}, \gamma_{vf^+}$ , and  $\gamma_{vv}$  fall to zero because of the conditions  $E_i' < \xi + \varepsilon_f$ ,  $E_i' < \xi + \varepsilon_f$ ,  $E_i' < \xi + \varepsilon_{f^+}$ ,  $E_i' < \xi + \varepsilon_{f^+}$ , and  $E_i' < 2\xi$ , respectively, as shown in Table III. The values of  $\gamma_{vv}$  for Ar, Kr, Ar<sub>2</sub>, and Kr<sub>2</sub> ions are also zero because of the condition  $E_i' < 2\xi$ . The values of  $\gamma_{f^+v}, \gamma_{vf^+}$  for  $\mathrm{Kr}_2$  ions are similarly zero because of the condition  $E'_i < \xi + \varepsilon_{f^+}$ .

Fig. 2(b) shows a schematic diagram of Auger deexcitation of an excited atom or molecule at the MgO surface that includes

TABLE IV CALCULATED  $\gamma$  Values Based on Auger Deexcitation for the Valence Band and the F and  $F^+$  Bands of MgO for Excited Rare-Gas Atoms and Molecules

|                                       | (eV)  | $\gamma_{\!f}$ | $\gamma_{f^+}$ | $\gamma_{_{\!\scriptscriptstyle  u}}$ |
|---------------------------------------|-------|----------------|----------------|---------------------------------------|
| He $E'_m$                             | 19.81 | 0.472          | 0.461          | 0.406                                 |
| $He_2 E_m^{\prime*}$                  | 17.79 | 0.469          | 0.456          | 0.392                                 |
| Ne $E'_m$                             | 16.61 | 0.466          | 0.452          | 0.382                                 |
| $Ne_2 E_m^{\prime*}$                  | 16.07 | 0.465          | 0.450          | 0.376                                 |
| Ar $E'_m$                             | 11.55 | 0.449          | 0.425          | 0.276                                 |
| $Ar_2 E_m^{\prime*}$                  | 10.86 | 0.445          | 0.419          | 0.259                                 |
| $Kr E'_m$                             | 9.91  | 0.439          | 0.409          | 0.226                                 |
| $Kr_2 E_{"}^{\prime *}$               | 8.49  | 0.426          | 0.386          | 0.133                                 |
| $\operatorname{Kr}_2 E_m^{\prime **}$ | 9.34  | 0.435          | 0.401          | 0.198                                 |
| $Xe E'_m$                             | 8.31  | 0.424          | 0.382          | 0.112                                 |
| $Xe_2 E_m^{\prime*}$                  | 7.17  | 0.408          | 0.349          | 0                                     |
| Xe <sub>2</sub> E'**                  | 8.16  | 0.422          | 0.379          | 0.092                                 |

the F and  $F^+$  bands. The secondary electron emission yields  $\gamma^D$  derived from these transitions were calculated using (9). Table IV shows the calculated  $\gamma^D$  values, based on Auger deexcitation between the valence band, and the F and  $F^+$  bands of MgO for metastable He, Ne, Ar, Kr, Xe atoms and He<sub>2</sub>, Ne<sub>2</sub>, Ar<sub>2</sub>, Kr<sub>2</sub>, Xe<sub>2</sub> excimers. Here, as in Fig. 2(b), when an electron 1 in the excited state of atoms or molecules moves to the ground state and an electron 2 in the  $F^+$  band is excited at the same time, the symbol of this secondary electron emission yield is represented by  $\gamma_{f^+}$ , for example. The symbols of the other secondary electron emission yields are also represented by similar procedures. As for the  ${\rm Kr_2}$  and  ${\rm Xe_2}$  excimers, not only the values of  $\gamma^D$  for  $E_m'^*$  (energy of the central wavelength in the lowest continuous spectrum at a distance s from the MgO surface), but also those of  $\gamma^D$  for  ${E'_m}^{**}$  (energy of the central wavelength in the second-lowest continuous spectrum at a distance s from the MgO surface) were calculated. The calculations of  $\gamma^D$  were made on the assumption that the values of  $E_m', {E_m'}^*$ , and  ${E_m'}^{**}$  are equal to those of energy in free space. The values of  $E_m'$  for metastable He, Ne, Ar, Kr, and Xe atoms

TABLE  $\,$  V Calculated  $\gamma$  Values Base d on Auger Neutralization of MgO for Rare-Gas Ions

| Gas                       | Не    | He <sub>2</sub> | Ne    | Ne <sub>2</sub> | Ar     | Ar <sub>2</sub> | Kr     | Kr <sub>2</sub> | Xe      | Xe <sub>2</sub> |
|---------------------------|-------|-----------------|-------|-----------------|--------|-----------------|--------|-----------------|---------|-----------------|
| $\gamma_{\min}^N$         | 0.329 | 0.307           | 0.257 | 0.256           | 0      | 0               | 0      | 0               | 0       | 0               |
| $\gamma_{\mathrm{max}}^N$ | 0.349 | 0.330           | 0.287 | 0.286           | 0.0484 | 0.0448          | 0.0371 | 0.00563         | 0.00292 | 0.00198         |

TABLE VI CALCULATED  $\gamma$  Values Base d on Auger Deexcitation of MgO for Excited Rare-Gas Atoms and Molecules

| Gas                 | Не    | He <sub>2</sub> | Ne    | Ne <sub>2</sub> | Ar    | Ar <sub>2</sub> | Kr    | Kı        | ŗ <sub>2</sub> | Xe    | Xe        | $e_2$      |
|---------------------|-------|-----------------|-------|-----------------|-------|-----------------|-------|-----------|----------------|-------|-----------|------------|
|                     |       |                 |       |                 |       |                 |       | $E_m^*$ , | $E_m^{**}$     |       | $E_m^*$ , | $E_m^{**}$ |
| $\gamma_{\min}^{D}$ | 0.406 | 0.392           | 0.382 | 0.376           | 0.276 | 0.259           | 0.226 | 0.133     | 0.198          | 0.112 | 0         | 0.092      |
| $\gamma_{ m max}^D$ | 0.412 | 0.399           | 0.389 | 0.384           | 0.292 | 0.276           | 0.245 | 0.160     | 0.219          | 0.140 | 0.0367    | 0.122      |

are 19.81, 16.61, 11.55, 9.91, and 8.31 eV, respectively [6]. The values of  $E_m{}'^*$  for He<sub>2</sub>, Ne<sub>2</sub>, Ar<sub>2</sub>, Kr<sub>2</sub>, and Xe<sub>2</sub> excimers are 17.79, 16.07, 10.86, 8.49, and 7.17 eV, respectively [17], [18]. The values of  $E_m{}'^*$  for Kr<sub>2</sub> and Xe<sub>2</sub> excimers are 9.34 and 8.16 eV, respectively. As for  $E_m{}'^*$  of Xe<sub>2</sub> excimer, the value of  $\gamma_v$  falls to zero because of the condition  $E_m{}'^* < \xi$ , as shown in Table IV.

According to time-dependent perturbation theory [3], the probabilities of transitions are expected to be proportional to the density of states [7]. Therefore, the densities of the F and  $F^+$  bands for MgO are assumed to be proportional to the CL intensities from the F and  $F^+$  bands. Based on this assumption, the  $\gamma^N$  and  $\gamma^D$  values of MgO, which include the F and  $F^+$  centers, are respectively obtained as follows:

$$\gamma^{N} = (P_{f}R_{f})^{2}\gamma_{ff} + (P_{f+}R_{f+})^{2}\gamma_{f+f+} + P_{v}^{2}\gamma_{vv} + (P_{f}R_{f}P_{f+}R_{f+})(\gamma_{ff+} + \gamma_{f+f}) + (P_{f}R_{f}P_{v})(\gamma_{fv} + \gamma_{vf}) + (P_{f+}R_{f+}P_{v})(\gamma_{f+v}\gamma_{vf+})$$
(11)

$$\gamma^D = P_f R_f \gamma_f + P_{f^+} R_{f^+} \gamma_{f^+} + P_v \gamma_v \tag{12}$$

where  $P_fR_f+P_{f^+}R_{f^+}+P_v=1$ ;  $R_f$  and  $R_{f^+}$  represent, respectively, normalized density of the F and  $F^+$  bands for MgO;  $P_v,P_f$ , and  $P_{f^+}$  represent the density ratios of the valence band,  $R_f$  and  $R_{f^+}$ , to the total density.

### IV. RESULTS AND DISCUSSION

The  $\gamma^N$  values of He, Ne, Ar, Kr, and Xe ions of atoms and molecules for an MgO film, deposited under the optimum conditions for the highest  $\gamma$  values, were calculated using (11) and the calculated values in Table III. In this calculation, it was determined that the values of  $R_f, R_{f^+}, P_f$ , and  $P_{f^+}$  were 0.45, 1, 0.01, and 0.1, respectively, by adjusting to fit the experimental results from CL spectra [10]. These calculated  $\gamma^N$  values are probably the highest  $\gamma^N_{\max}$  values of MgO. Table V shows the results obtained. Here,  $\gamma^N$  values of MgO without defect states also shown; these  $\gamma^N$  values are equal to  $\gamma_{vv}$  values in Table III. These calculated  $\gamma^N$  values are probably the lowest  $\gamma^N_{\min}$  values of MgO.

The  $\gamma^D$  values of metastable He, Ne, Ar, Kr, Xe atoms and He<sub>2</sub>, Ne<sub>2</sub>, Ar<sub>2</sub>, Kr<sub>2</sub>, Xe<sub>2</sub> excimers for MgO film deposited under

the optimum conditions for the highest  $\gamma$  values were also calculated using (12) and the calculated values in Table IV. These calculated  $\gamma^D$  values are probably the highest  $\gamma^D_{\max}$  values of MgO. Table VI shows the results obtained. Here,  $\gamma^D$  values for MgO without defect states also shown; these  $\gamma^D$  values are equal to  $\gamma_v$  values in Table IV. These calculated  $\gamma^D$  values are probably the lowest  $\gamma^D_{\min}$  values of MgO.

As mentioned above, we also have to consider the electron emission process: resonance neutralization + Auger deexcitation. The resonance neutralization cannot occur with the combinations of the band parameters for MgO (see Table II) and rare-gases shown in Tables III and IV, except for Ne and Xe2 ions. Therefore, the  $\gamma_i$  values of MgO for rare-gas ions, except Ne and Xe2 ions, are determined by Auger neutralization only, namely  $\gamma_i=\gamma^N$  in Table V. The resonance neutralization for Ne and Xe2 ions can occur because of the conditions  $\varepsilon_f \leq E_i' - E_m' \leq \varepsilon_f + 0.3$  and  $\varepsilon_f \leq E_i' - E_m' \leq \varepsilon_f + 0.3$ , respectively. The  $\gamma_i$  values for Ne and Xe2 ions were calculated using (6) on the assumption that  $1-g=(1/2)R_fP_f$ . The calculated  $\gamma_i$  values for Ne and Xe2 ions are 0.287 and 0.002 06; the calculated  $\gamma^N$  values for Ne and Xe2 ions are 0.287 and 0.001 98. Therefore,  $\gamma$  values of the MgO for Ne and Xe2 ions are also almost completely determined by Auger neutralization only.

On the other hand, in the secondary electron emission yield  $\gamma_m$  by metastable atoms or excimers, this  $\gamma^D$  is considered to be the main component, namely,  $\gamma_m = \gamma^D$  in Table VI.

The  $\gamma^N_{\min}$  values of Ar, Kr, and Xe ions of atoms and molecules for MgO fall to zero because of the condition  $E_i' < 2\xi$ . The  $\gamma^D_{\min}$  value of the Xe<sub>2</sub> excimer  $({E_m'}^*)$  for MgO falls to zero because of the condition  ${E_m'}^* < \xi$ . The difference between  $\gamma^N_{\max}$  and  $\gamma^N_{\min}$  values decreased with increasing  $E_i'$  values of ions, because the  $\gamma^N$  values for large  $E_i'$  values of ions are determined by the Auger transitions, which occur principally in the valence band. On the other hand, the difference between  $\gamma^D_{\max}$  and  $\gamma^D_{\min}$  values also decreased with increasing  $E_m'$  values of metastable atoms and excimers, because the  $\gamma^D$  values for large  $E_m'$  values of metastable atoms and excimers are determined by the Auger transitions, which occur principally in the valence band.

Ref. 23

Ref. 24

0.14

| <b>VV</b> 1              | IH LAFEKIME | NIAL 7i VALU | E3 I KOM IF | ie Literati | KE      |
|--------------------------|-------------|--------------|-------------|-------------|---------|
| Gas                      | Не          | Ne           | Ar          | Kr          | Xe      |
| $\gamma_{i \text{ min}}$ | 0.329       | 0.257        | 0           | 0           | 0       |
| $\gamma_{i \max}$        | 0.349       | 0.287        | 0.0484      | 0.0371      | 0.00292 |
| Ref. 19                  | -           | 0.45         | 0.05        | -           | -       |
| Ref. 20                  | -           | 0.25         | -           | -           | 0.035   |
| Ref. 21                  | 0.17-0.35   | 0.06-0.17    | ≤ 0.05      | ≤0.015      | ≤0.007  |
| Ref. 22                  | 0.13        | 0.3          | 0.009       | 0.009       | 0.002   |

0.5

0.12

0.03

0.06

0.003

0.04

TABLE VII COMPARISONS OF THE THEORETICALLY CALCULATED  $\gamma_i$  Values of MgO WITH EXPERIMENTAL  $\gamma_i$  Values From the Literature

The  $\gamma^N$  values of ions of atoms are a little larger than those of molecules, as shown in Table V. The  $\gamma^D$  values of metastable atoms are also a little larger than those of excimers, as shown in Table VI.

As for rare-gas ions of atoms, the experimental  $\gamma_i$  values of MgO have been previously reported. Table VII shows the comparisons between our results and the experimental results. The results of six experiments are shown in Table VII; in three of those the  $\gamma_i$  values were measured using an ion beam [19], [21], [24]: the rest were estimated from breakdown voltages in gas [20], [22], [23]. In general, measurement of  $\gamma_i$  for MgO is not always easy because of the possible difficulties due to the charge-up effect and adsorption on a surface of a sample. Here, although the measured  $\gamma_i$  values are not always the same between the experiments, their tendency to vary, depending on the kind of gas ion, agrees well with our results.

### V. CONCLUSION

The  $\gamma^N$  values of He, Ne, Ar, Kr, and Xe ions of atoms and molecules for an MgO film, deposited under the optimum conditions, were calculated, assuming Auger transitions between the valence band, and the F and  $F^+$  centers in the MgO surface. The  $\gamma^D$  values of metastable He, Ne, Ar, Kr, Xe atoms and He<sub>2</sub>, Ne<sub>2</sub>, Ar<sub>2</sub>, Kr<sub>2</sub>, Xe<sub>2</sub> excimers for an MgO film deposited under the optimum conditions were also calculated. These calculated  $\gamma^N$  and  $\gamma^D$  values are probably the same as those used for MgO in practice. All the calculated  $\gamma$  values fall to nonzero with combinations of MgO and these rare-gas particles, whereas the  $\gamma^N$  values of Ar, Kr, and Xe ions of atoms and molecules for MgO without defect states fall to zero. The  $\gamma^D$  value of Xe<sub>2</sub> excimer  $(E_m^*)$  for MgO without defect states also falls to zero. These calculated  $\gamma^N$  and  $\gamma^D$  values for MgO without defect states are probably the lowest values theoretically.

Resonance neutralization cannot occur with the combinations of MgO deposited under the optimum conditions and these rare-gas particles, with the exception of Ne and Xe<sub>2</sub> ions. For Ne and Xe<sub>2</sub> ions, the difference between the calculated values of  $\gamma_i$  and  $\gamma^N$  was small. Therefore,  $\gamma$  values of the MgO

for Ne and Xe<sub>2</sub> ions are also almost completely determined by Auger neutralization only, namely  $\gamma_i = \gamma^N$ .

The difference between  $\gamma^N$  values of MgO deposited under the optimum conditions and those of MgO without defect states decreases with increasing ionization energy of ions because the  $\gamma^N$  values for ions possessing large ionization energy are determined by Auger transitions, which occur principally in the valence band. On the other hand, the difference between the  $\gamma^D$  values of MgO deposited under the optimum conditions and those of MgO without defect states also decreases with increasing excitation energy of metastable atoms and excimers because the  $\gamma^D$  values for metastable atoms and excimers which have large excitation energy are determined by Auger transitions which occur principally in the valence band.

The  $\gamma^N$  values of ions of atoms are a little larger than those of molecules. The  $\gamma^D$  values of metastable atoms are also a little larger than those of excimers.

As for rare-gas ions of atoms, the calculated  $\gamma_i$  values were compared with experimental results reported previously. Here, although the measured  $\gamma_i$  values are not always the same between the experiments, their tendency to vary, depending on the kind of gas ion, agrees well with our results.

These results will be useful for investigating the mechanism of discharge of PDPs in further detail.

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Yasushi Motoyama received the B.E. and M.E. degrees in electrical information engineering from Yokohama National University, Yokohama, Japan, in 1984 and 1986, respectively.

In 1986, he joined NHK (Japan Broadcasting Corporation). Until 1989, he was with the NHK Niigata Broadcasting Station, Niigata Prefecture. Since then, he has been working at the Science and Technical Research Laboratories of NHK, Tokyo, and has been engaged in research of plasma display devices.

Mr. Motoyama is a member of the Institute of

Image Information and Television Engineers and the Society for Information Display.



**Fumio Sato** received the B.E. degree and the Ph.D. degree in materials engineering from Tohoku University, Tohoku, Japan, in 1974 and 1977, respectively.

In 1977, he joined NHK (Japan Broadcasting Corporation) Science and Technical Research Laboratories, Tokyo. He has been engaged in research and development on crystal growth of semiconductors, X-ray process, photoconductive materials, and field emitter materials.

Dr. Sato is a member of the Japan Society of Applied Physics, the Institute of Image Information and

Television Engineers, and the Institute of Electrical Engineers of Japan.